

Switching to spherical coordinates we set up the integral as

$$\begin{aligned} & \int_0^{2\pi} \int_0^\pi \int_0^{\sqrt{2}} \rho^2 \cdot \rho^2 \sin \phi d\rho d\phi d\theta \\ & \int_0^{2\pi} \int_0^\pi \int_0^{\sqrt{2}} \rho^4 \sin \phi d\rho d\phi d\theta \\ & = \int_0^{2\pi} \int_0^\pi \frac{(\sqrt{2})^5}{5} \sin \phi d\phi d\theta \\ & = \frac{4\sqrt{2}}{5} \int_0^{2\pi} (-\cos \phi)|_0^\pi d\theta \\ & = \frac{4\sqrt{2}}{5} \cdot 2 \cdot 2\pi = \frac{16\pi\sqrt{2}}{5}. \end{aligned}$$