

Parametrize the path as  $2 \cos t \mathbf{i} + 2 \sin t \mathbf{j}$ ,  $0 \leq t \leq \pi$ , followed by  $t \mathbf{i}$ ,  $-2 \leq t \leq 2$ . The work is

$$\begin{aligned} \int_C \mathbf{F} \cdot d\mathbf{R} &= \int_0^\pi [2(2 \cos t)^2 + 2(2 \sin t)^2](-2 \sin t) dt \\ &+ \int_0^\pi [3(2 \cos t) + 3(2 \sin t)](2 \cos t) dt + \int_{-2}^2 (2t^2) dt \\ &= \int_0^\pi 8(\cos^2 t + \sin^2 t)(-2 \sin t) dt + \int_0^\pi (12 \cos^2 t + 12 \sin t \cos t) dt + \frac{2t^3}{3} \Big|_{-2}^2 \\ &= \int_0^\pi (-16 \sin t) dt + \int_0^\pi (6(\cos 2t + 1) + 6 \sin 2t) dt + \frac{32}{3} \\ &= -32 + 6\pi + \frac{32}{3} = 6\pi - \frac{64}{3}. \end{aligned}$$